

IDENTIFICATION IN DYNAMIC NETWORKS

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Abstract

System identification is a common tool for estimating (linear) plant models as a basis for model-based predictive control and optimization. The current challenges in process industry, however, ask for data-driven modelling techniques that go beyond the single unit/plant models. While optimization and control problems become more and more structured in the form of decentralized and/or distributed solutions, the related modelling problems will need to address structured and interconnected systems. An introduction will be given to the current state of the art and related developments in the identification of linear dynamic networks. Starting from classical prediction error methods for open-loop and closed-loop systems, several consequences for the handling of network situations will be presented and new research questions will be highlighted.

Keywords

system identification, dynamic networks, identifiability, experiment design, model-based control, distributed control, closed-loop identification.

1 Introduction

System identification is a well-developed technology for estimating plant models from operational data, typically taken during dedicated plant testing/excitation. Data-driven estimation and maintenance of dynamic models is considered a key technology for realizing a higher level of autonomy of model-based controllers when maintaining economic optimal operation of the plant, see e.g. Gevers (2005); Zhu (2006); Darby and Nikolaou (2014); Özkan et al. (2016).

The system configurations that are typically being considered are either multivariable open-loop or feedback controlled (closed-loop) systems. Whereas in open-loop identification the plant input signals are not restricted by the system, in closed-loop systems the presence of feedback induces a correlation of the plant's output disturbances with the plant input, thereby complicating the identification problem, see e.g. Ljung (1999). This has led to the development of dedicated closed-loop identification schemes.

In several areas of technology, the development of controlling and optimizing system's operations, involves the handling of structure and of interacting subsystems.

This is happening in solutions for decentralized and distributed process control, see e.g. Rawlings and Stewart (2008); Christofides et al. (2013). Also in other technology domains, like power networks and robotic networks, interconnection structures are playing an increasing role, while in areas like systems biology the modelling and identification of interconnected systems, including the topology, is a key problem.

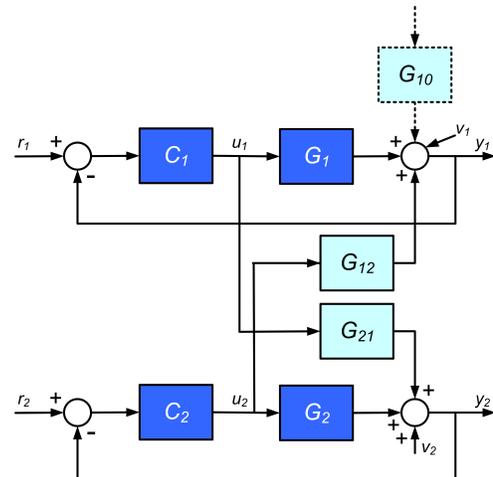


Figure 1. Interacting dynamics in two control loops

A nice example of a structured identification prob-

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lem is the problem of two interconnected controlled systems, as present in Figure 1, which is considered in Gudi and Rawlings (2006), for the particular situation that $G_{12} = 0$, and where the identification problem is to identify the interacting dynamics G_{21} and possibly G_{12} . The handling of such structured systems should be facilitated by a theory for identification in dynamic networks, which is lacking in the classical identification literature. In this paper several steps in the recent development of such a theory are highlighted and illustrated.

2 Linear dynamic networks

Following the basic setup of Van den Hof et al. (2013), a dynamic network is built up out of L scalar *internal variables* or *nodes* w_j , $j = 1, \dots, L$, and K *external variables* r_k , $k = 1, \dots, K$. Each internal variable is described as:

$$w_j(t) = \sum_{\substack{l=1 \\ l \neq j}}^L G_{jl}^0(q)w_l(t) + r_j(t) + v_j(t) \quad (1)$$

where q^{-1} is the delay operator, i.e. $q^{-1}w_j(t) = w_j(t-1)$;

- G_{jl}^0 , are proper rational transfer functions, and the single transfers G_{jl}^0 are referred to as *modules* in the network.
- r_k are *external variables* that can directly be manipulated by the user;
- v_j is *process noise*, where the vector process $v = [v_1 \dots v_L]^T$ is modelled as a stationary stochastic process with rational spectral density, such that there exists a p -dimensional white noise process $e := [e_1 \dots e_p]^T$ with diagonal covariance matrix $\Lambda^0 > 0$ and $p \leq L$, such that $v(t) = H^0(q)e(t)$, with H^0 a proper rational transfer function matrix that is monic and stable and has a stable left inverse.

A single building block of the network is depicted in Figure 2.

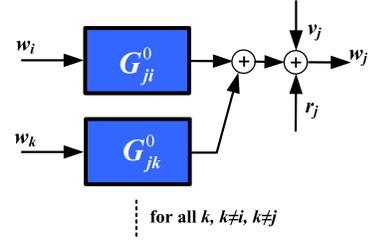


Figure 2. Node building block of a network

The situation that we would like to consider is the full network constructed by combining (1) for all node signals,

$$\begin{bmatrix} w_1 \\ w_2 \\ \vdots \\ w_L \end{bmatrix} = \begin{bmatrix} 0 & G_{12}^0 & \cdots & G_{1L}^0 \\ G_{21}^0 & 0 & \ddots & \vdots \\ \vdots & \vdots & \ddots & G_{L-1, L}^0 \\ G_{L1}^0 & \cdots & G_{L, L-1}^0 & 0 \end{bmatrix} \begin{bmatrix} w_1 \\ w_2 \\ \vdots \\ w_L \end{bmatrix} + R^0 \begin{bmatrix} r_1 \\ r_2 \\ \vdots \\ r_K \end{bmatrix} + H^0 \begin{bmatrix} e_1 \\ e_2 \\ \vdots \\ e_p \end{bmatrix}$$

Using obvious notation this results in the matrix equation:

$$w = G^0(q)w + R^0(q)r + H^0(q)e. \quad (2)$$

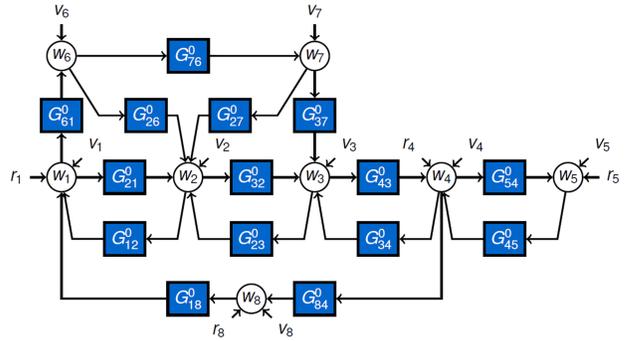


Figure 3. Example of a dynamic network

3 Identification of a single module - the full MISO approach

3.1 Direct method

When the objective is to identify a single module in the network, denoted as G_{ji}^0 , while the topology of the network is known, then there is a direct identification algorithm that can provide a consistent estimate of this module dynamics. To this end the following additional assumptions are formulated:

- The spectral density $\Phi_v(\omega)$ is diagonal, i.e. all noise signals are mutually uncorrelated;
- Every loop around node signal w_j has a delay (no algebraic loops);

Next we will formulate the algorithm, which is a direct generalization of the classical direct method for closed-loop identification (Van den Hof et al. (2013)):

1. Determine the set \mathcal{N}_j of all node numbers k such that $G_{jk}^0 \neq 0$; all node signals in this set need to be measured, besides w_j ;
2. Determine the subset $\mathcal{K}_j \subset \mathcal{N}_j$ of all node numbers k such that G_{jk}^0 is known a priori;
3. Denote $\mathcal{U}_j = \mathcal{N}_j \setminus \mathcal{K}_j$, as the set of node signals k for which G_{jk}^0 needs to be estimated;
4. Determine $\bar{w}_j(t) := w_j(t) - r_j(t) - \sum_{k \in \mathcal{K}_j} G_{jk} w_k(t)$
5. Solve the identification problem

$$\hat{\theta}_N := \arg \min_{\theta} \frac{1}{N} \sum_{t=0}^{N-1} \varepsilon^2(t, \theta), \quad \text{with}$$

$$\varepsilon(t, \theta) := H_j(\theta)^{-1} [\bar{w}_j(t) - \sum_{k \in \mathcal{U}_j} G_{jk}(\theta) w_k(t)]. \quad (3)$$

Then $G_{jk}(\hat{\theta}_N)$, $k \in \mathcal{U}_j$ and $H_j(\hat{\theta}_N)$ are estimated consistently, provided that the model set is parametrized so as to contain the real underlying system (system in the model set), and the input signals of the estimated modules $G_{jk}(\theta)$ are sufficiently informative.¹

When applying this algorithm to the example network in Figure 3, and the objective would be to identify the module G_{21}^0 , then $\mathcal{N}_2 = \{1, 3, 6, 7\}$. If all the corresponding modules are unknown, they need to be identified, leading to a 4-input, 1-output identification problem. The consistent estimation of the target module G_{21}^0 is then embedded in the consistent estimation of all 4 modules in the considered MISO system.

3.2 Two-stage / projection approach

Whereas the direct identification method requires exact noise modelling in order to arrive at consistent module estimates, a second approach, called the two-stage or projection approach, allows to estimate module dynamics independently from noise models. Rather than using measured node signals as model inputs, this method uses projected node signals, i.e. node signals that are projected onto external excitation signals r_i , as introduced in Van den Hof and Schrama (1993) for classical closed-loop identification problems.

The algorithm from the previous subsection is now adapted as follows:

1. Select a set of excitation signals $\{r_m\}$, with $m \in \mathcal{R}_{is}$ that are correlated with w_i .
2. Denote $\mathcal{U}_{is} \subset \mathcal{U}_j$ as the set of node signals that is correlated to any of the excitation signals in \mathcal{R}_{is} .
3. Determine the projected signals $w_k^{(\mathcal{R}_{is})}$, for $k \in \mathcal{U}_{is}$. This can be done through correlation techniques, or through an estimation procedure, according to Van den Hof and Schrama (1993).
4. Proceed with steps 4-5 above, with the prediction error

$$\varepsilon(t, \theta) := H_j(\eta)^{-1} [\bar{w}_j(t) - \sum_{k \in \mathcal{U}_{is}} G_{jk}(\theta) w_k^{(\mathcal{R}_{is})}(t)].$$

Then $G_{jk}(\hat{\theta}_N)$, $k \in \mathcal{U}_{is}$ are estimated consistently, provided that the model set is parametrized so as to contain the real underlying system (modules in the model set), and the projected input signals $w_k^{(\mathcal{R}_{is})}$ are sufficiently informative.²

When applying this algorithm to the example of Figure 3, and focussing again on estimating module G_{21}^0 , then, when choosing the external signal r_1 , so $\mathcal{R}_{is} = \{1\}$, it follows that $\mathcal{U}_{is} = \{1, 3, 6, 7\}$. So again we will have a 4-input, 1-output identification problem. However when all input signals are projected onto r_1 , the resulting signals might not be sufficiently informative. In order to reach this, an option to include the external signals r_4, r_5 and r_8 too, leading to $\mathcal{R}_{is} = \{1, 4, 5, 8\}$. The network topology conditions on the excitation signals r_m , i.e. the possible correlations with node signals, can be verified by algorithms from graph theory.

4 Predictor input selection

4.1 Direct method

The methods discussed in the previous section include basically all potential node signals as inputs in the predictor models. Including all possible inputs is typically not necessary, leading to the opportunity to make a more sparse selection. This can be of importance if some node signals in the network are hard (or expensive) to measure. The methods presented below originate from Dankers et al. (2016).

We are going to construct a set $\mathcal{D}_j \subset \mathcal{U}_j$, being a set of node variables that will serve as predictor inputs.³

¹More detailed conditions for informativity of the data are explored in Gevers and Bazanella (2015).

²For the two-stage / projection approach the condition on absence of algebraic loops around w_j can be removed.

³It is actually not strictly necessary that $\mathcal{D}_j \subset \mathcal{U}_j$.

In view of the consistent identification of the module G_{ji}^0 , a relaxed set of conditions that needs to be satisfied for this set \mathcal{D}_j can be formulated as follows:

- (a) $i \in \mathcal{D}_j, j \notin \mathcal{D}_j$;
- (b) every path w_i to w_j , excluding the path G_{ji}^0 , goes through a node $w_k, k \in \mathcal{D}_j$;
- (c) every loop through w_j goes through a node $w_k, k \in \mathcal{D}_j$.

These conditions state that every path that is parallel to G_{ji}^0 and every loop around w_j should be blocked by a predictor input. If these conditions are satisfied for \mathcal{D}_j , then a reduced (immersed) network can be constructed composed of node signals $\{j, \mathcal{D}_j\}$. The immersed network is a network in which a particular set of nodes is removed, and therefore a network with a reduced set of node signals remains. However the node signals that remain are invariant, i.e. they are exactly the same signals as in the original network. This immersed network will have module dynamics $\check{G}_{jk}^0, k \in \mathcal{D}_j$, that in general will be different from the original module dynamics, while the node signals remain invariant. However under the conditions listed above it holds that $G_{ji}^0 = \check{G}_{ji}^0$, and therefore in the immersed network we can still identify the intended module G_{ji}^0 .

In order to guarantee consistency of the module estimate, one additional conditions needs to be satisfied, which is related to the notion of confounding variables.

In the current setup of output variable w_j and a set \mathcal{D}_j of predictor inputs, a variable v_ℓ is called a *confounding variable* if it directly affects the output w_j as well as at least one of the inputs $w_k, k \in \mathcal{D}_j$. Formally stated, v_ℓ is a confounding variable if there exists an input node $k \in \mathcal{D}_j$ such that there exist paths from v_ℓ to w_k and from v_ℓ to w_j that do not pass through a node in $\{j, \mathcal{D}_j\}$. Confounding variables are non-measured variables that affect both input and output, and create correlation between the two signals that is not generated by module dynamics.

The direct MISO identification method of section 3.1 can then be applied with the predictor input set $w_k, k \in \mathcal{D}_j$. Under the usual conditions, listed in Section 3.1, the module G_{ji}^0 is estimated consistently provided that no disturbance signal v_ℓ is a confounding variable.

If we return to the example of Figure 3 and the modelling of G_{21}^0 , it follows that in order to satisfy conditions (a)-(c) above, it would suffice to choose $\mathcal{D}_j = \{1, 3, 6\}$. In comparison with the previous section, node signal w_7 is not necessary as a predictor input for the immersed

network to maintain G_{21}^0 . However in this setting, w_7 now acts as a confounding variable, since it has a path to input w_3 and output w_2 . This confounding variable can be “blocked” by including w_7 as a predictor input into \mathcal{D}_j , as in that situation w_7 is no longer a confounding variable. As a result, we have not been able to effectively reduce the set of predictor inputs in this particular case.

4.2 Two-stage / projection approach

A similar result as in the previous section can be formulated for the two-stage / projection approach, but with slightly varying conditions. The most important difference being that for this method the presence of confounding variables is no problem for consistency. The selection of input nodes \mathcal{D}_j needs to satisfy conditions (a)-(c) from the previous section, in order to guarantee the correct dynamics being present in \check{G}_{ji}^0 .

Let $\{r_m\}, m \in \mathcal{T}_j$ be the external excitation signals onto which the input node signals $\{w_k\}, k \in \mathcal{D}_j$ will be projected, denoted as $w_k^{\mathcal{T}_j}$.

Then application of the two-stage / projection method, on the basis of the prediction error:

$$\varepsilon(t, \theta) := \check{H}_j(\eta)^{-1}[\bar{w}_j(t) - \sum_{k \in \mathcal{D}_j} \check{G}_{jk}^0(\theta)w_k^{\mathcal{T}_j}(t)]$$

will lead to a consistent estimate of $\check{G}_{ji}^0 = G_{ji}^0$, under conditions that are similar to the formulations in Section 3.2, while additionally there should not exist external signals that are selected in \mathcal{T}_j that have paths to w_j that do not pass through nodes in \mathcal{D}_j . Such external excitation signals would then act as a disturbance on the output that is correlated with the inputs.

When applying this result to the situation of the dynamic network in Figures 3 and 4, we can choose $\mathcal{D}_j = \{1, 3, 6\}$ as predictor inputs, while all reference signals can be used for projection, i.e. $\mathcal{T}_j = \{1, 4, 5, 8\}$. The fact that v_7 is a confounding variable is no limitation now, and thus w_7 does not need to be included as a predictor input, and so does not need to be measured. The signals that need to be measured are indicated in green in Figure 4.

5 Module identification with sensor noise

It is often the case that the variables w_k in (1) are measured using sensors. The measurement error that results from imperfect sensor readings is called *sensor noise* and denoted s_k . The measured version of the in-

- There must be a delay in the path from w_j to the instrumental variables w_ℓ , $\ell \in \mathcal{I}_j$.

When considering the dynamic networks in Figure 5, and the objective is to estimate G_{32}^0 , then the classical treatment of an instrumental variable method would work for situation (a), where \tilde{w}_1 could be chosen as an instrumental variable in a typical linear regression scheme, that requires the IV-signal to be correlated to the input signal (in this case w_2), but not correlated to the output noise v_3 . In the system depicted in Figure 5(b) this latter condition is not satisfied. However the dynamic network method discussed in this section would also work in case (b), when choosing \tilde{w}_1 as IV-signal, provided that there is a delay in G_{13}^0 .

The overall observation is that in a dynamic network, sensor noise is more easily dealt with than in a simple open-loop or closed-loop system, simply because of the presence of multiple signals that can be used to extract the relevant information.

6 Network identifiability

When we move from the (local) identification of a single module to the (global) identification of either the dynamics or the topology of the full network, other questions have to be addressed. It also has to be noted that local identification of a module through estimating a MISO model, can only be justified (from a minimum variance perspective) if the process noises on the different node signals are uncorrelated.

In handling the full network, we will expand the assumption on the process noise, to allow for correlation over the different nodes, thus allowing $\Phi_v(\omega)$ to be non-diagonal.

When identifying the full network dynamics in that situation, one of the important questions is whether the dynamic network is uniquely represented in the model set that is chosen. E.g. if we allow transfer functions to appear between all node signals available, can we then uniquely identify the network? It can be expected that the answer to this question will be related to the type of excitation that is present in the network.

We will consider a network model set, to be defined as

$$\mathcal{M} := \{(G(\theta), H(\theta), R(\theta)), \theta \in \Theta\}$$

where a network model is represented by the triplet $M(\theta) = (G(\theta), H(\theta), R(\theta))$.

The network transfer function is denoted by

$$T^0 := [I - G^0]^{-1} \begin{bmatrix} H^0 & R^0 \end{bmatrix},$$

reflecting the mapping from external signals e and r to node signals w . T^0 is the (MIMO) transfer function that can generally be uniquely identified from measured data, provided that the external excitation signals are sufficiently informative.

The question of network identifiability addresses the topic whether two different models in \mathcal{M} have the same network transfer function. The model set \mathcal{M} will be called *network identifiable* (Weerts et al., 2015), if for any two models $M(\theta_1)$ and $M(\theta_2)$ in \mathcal{M} it holds that

$$\{T(\theta_1) = T(\theta_2)\} \implies \{M(\theta_1) = M(\theta_2)\}.$$

Note that network identifiability is referring to a property of the model set formulated in terms of properties of the models M , rather than the parameters θ . The model set \mathcal{M} can be chosen in different ways, depending on the structural conditions that we would like to impose on the models. If all possible modules (connecting each and every node in the network) are parametrized, then identifiability of the model set will require strong conditions on the excitation signals being present.

Under rather generic conditions on the model parametrizations (see Weerts et al. (2016)), network identifiability can be shown if the following conditions are satisfied:

1. Each row i of $\begin{bmatrix} G(\theta) & H(\theta) & R(\theta) \end{bmatrix}$ has at most $K + p$ parameterized entries, where K is the number of external excitation signals and p is the number of white noise processes driving the process noise v , and
2. For each row i , \check{T} has full row rank, where \check{T} is the submatrix of T composed of those rows j that correspond to elements $G_{ij}(\theta)$ in $G(\theta)$ that are parameterized.

The second condition is automatically satisfied whenever $\begin{bmatrix} H(\theta) & R(\theta) \end{bmatrix}$ has full row rank for all θ , being a situation which is guaranteed if each and every node signal has either an excitation signal r or an independent process disturbance v directly connected to it.

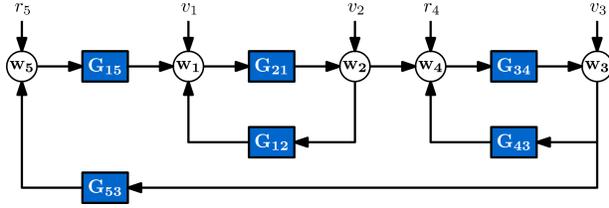


Figure 6. Five node dynamic network (Weerts et al., 2016).

As an example consider the dynamic network in Figure 6, with three process noises and two external excitations. We can consider three different situations now:

1. If the three noise terms are known to be uncorrelated, and the presence of r_4 and r_5 is known, then

$$\begin{bmatrix} H(\theta) & R(\theta) \end{bmatrix} = \begin{bmatrix} H_1(\theta) & 0 & 0 & 0 & 0 \\ 0 & H_2(\theta) & 0 & 0 & 0 \\ 0 & 0 & H_3(\theta) & 0 & 0 \\ 0 & 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 0 & 1 \end{bmatrix}$$

being of full row rank, implying that for any parametrization of $G(\theta)$, the model set is identifiable. This is caused by the independent excitation of each node of the network.

2. If v_1 and v_2 are known to be correlated, they have to be modelled in a multivariable way, leading to

$$\begin{bmatrix} H(\theta) & R(\theta) \end{bmatrix} = \begin{bmatrix} H_{11}(\theta) & H_{12}(\theta) & 0 & 0 & 0 \\ H_{21}(\theta) & H_{22}(\theta) & 0 & 0 & 0 \\ 0 & 0 & H_3(\theta) & 0 & 0 \\ 0 & 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 0 & 1 \end{bmatrix}$$

Since we do not have a guarantee anymore that this matrix is full row rank, we loose network identifiability if the network structure in $G(\theta)$ is fully parametrized. A fully parametrized $G(\theta)$ will be a 5×5 matrix with 4 parametrized transfers on each row. This implies that the first two rows of the matrix $\begin{bmatrix} G(\theta) & H(\theta) & R(\theta) \end{bmatrix}$ will have 6 parametrized entries, while the number of external signals $K+p = 5$. In this situation we loose identifiability.

3. If we consider the same situation, but now using information on the topology of the network, i.e. we parametrize

$$G(\theta) = \begin{bmatrix} 0 & G_{12}(\theta) & 0 & 0 & G_{15}(\theta) \\ G_{21}(\theta) & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & G_{34}(\theta) & 0 \\ 0 & 1 & G_{43}(\theta) & 0 & 0 \\ 0 & 0 & G_{53}(\theta) & 0 & 0 \end{bmatrix}$$

then the maximum number of parametrized entries in $\begin{bmatrix} G(\theta) & H(\theta) & R(\theta) \end{bmatrix}$ is 4 and the first condition for network identifiability is satisfied. It can be verified that in this case also the second condition is satisfied, and that network identifiability is guaranteed.

7 The interacting two-control loops

The situation of the interacting two control loops as sketched in Figure 1, has been treated in detail in Gudi and Rawlings (2006), with respect to the identification of the interacting dynamics G_{21} for the situation that $G_{12} = 0$. When considering this problem in the scope of the network identification approaches in the present paper, the following observations can be made:

- A direct way to identify G_{21} would be to model the two-input one-output system, having u_1 and u_2 as inputs and y_2 as output, and applying a direct identification method. Provided that u_1 and u_2 are sufficiently exciting, this would lead to a consistent estimate of G_{21} and G_2 , under the condition that an appropriate noise model is identified too.
- Alternatively the necessity to include a noise model could be relaxed by using a two-stage / projection approach where the input signals u_1 and u_2 are projected onto the external excitation signals r_1 and r_2 , as well as onto possible additional dither signals added to the plant inputs.

8 Discussion and challenges

We have presented a schematic picture on methods and tools, that are based on classical closed-loop identification schemes, that can be generalized to the situation of structured dynamic networks. Identification in/of dynamic networks is a challenging area for which many of the problems still need to be sorted out. Questions like: optimal locations of sensors and actuators in order to achieve a particular model accuracy, experiment design, and identifying the topology of networks on the basis of data, are just a few topics that can be mentioned in this sense. Additionally, while allowing to let the networks grow in dimensions, the scalability of algorithms will become an important topic.

Acknowledgments

This work has received funding from the European Research Council (ERC), Advanced Research Grant SYSDYNET, under the European Union's Horizon 2020 research and innovation programme (grant agreement No 694504). The authors acknowledge the discussions with and contributions of Xavier Bombois, Peter Heuberger and Jobert Ludlage.

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